

Alternative Proof

Suppose there were TM H that decided A_{tm} . Then one could use H as a subroutine to decide the language S_{tm} . But that language is not recursive. Contradiction.