

**In-class Practice 21: Closure Again**

Let  $A$  be an alphabet, and let  $f$  be a function that maps each symbol in  $A$  to some nonempty string. Given a string  $w$  in  $A^*$ , we define the string  $w^f$  as replacing every symbol in  $w$  by its corresponding  $f$  value. And we define for language  $L$  the language  $L^f$  as the set of all  $w^f$  for  $w$  in  $L$ .

(a) Show that if  $L$  is r.e. then so is  $L^f$ .

(b) Show (by means of an example) that  $L^f$  can be regular even if  $L$  is not.