

**Assignment 6**

**Part 1:** Write a two-page summary of (the portion of) the paper that you presented in class.

**Part 2:**

1. Give a formula for the sum of the squares of the eigenvalues of a graph.
2. (a) Define a good drawing of a graph in the plane as one where no two edges intersect more than once. Show that the crossing number of any graph is achieved by a good drawing.  
(b) Show that the crossing number of  $K_{2025,2025}$  is even by showing that every good drawing of it has an even number of crossings.
3. Show that the crossing number of  $K_3 \square C_n$  is at most  $n$  for all  $n \geq 3$ .

**Due: Tuesday April 22**